

## Summary of the derivatives and their uses:

Function	Use
$f(x)$	<ul style="list-style-type: none"> <li>- To find points on the curve/existence of points on the curve</li> <li>- Verify that the graph is continuous (has no breaks)</li> <li>- If the graph is not continuous, can determine these values and said values will be critical numbers</li> </ul>
$f'(x)$	<ul style="list-style-type: none"> <li>- Use typically to show <i>increasing</i> and <i>decreasing</i>.</li> <li>- If <math>f'(x) = 0</math>, and is solved for <math>x</math>, these will be some of the critical numbers.</li> <li>- With the critical numbers, can create an interval. With this interval, choose a test value (say <math>c</math>) between the critical numbers to substitute into <math>f'(x)</math>.</li> <li>- If <math>f'(c) &gt; 0</math> (positive) then the original function, <math>f(x)</math>, will be increasing between the critical numbers for which <math>c</math> was picked.</li> <li>- If <math>f'(c) &lt; 0</math> (negative) then the original function, <math>f(x)</math>, will be decreasing between the critical numbers for which <math>c</math> was picked.</li> <li>- <b>First Derivative Test:</b> If the original function, <math>f(x)</math>, switches from increasing to decreasing at a critical point, then it will be a <u>local max</u>. If the original function, <math>f(x)</math>, switches from decreasing to increasing at a critical point, then it will be a <u>local min</u>.</li> </ul>
$f''(x)$	<ul style="list-style-type: none"> <li>- If <math>f''(x) = 0</math> and is solved for <math>x</math>, these are <i>potential</i> points of inflection (where the concavity changes). To prove that they are indeed points of inflection, we need to look at the intervals of concavity</li> <li>- With the values from the first bullet, we can create intervals and take test values (<math>a</math>) between the potential points of inflection.</li> <li>- If <math>f''(a) &gt; 0</math> (positive) then the original function, <math>f(x)</math>, will be concave up (CCU) between the potential points of inflection for which <math>a</math> was picked.</li> <li>- If <math>f''(a) &lt; 0</math> (negative) then the original function, <math>f(x)</math>, will be concave down (CCD) between the potential points of inflection (<math>a</math>) for which <math>a</math> was picked.</li> <li>- If the concavity switches at one of the potential points of inflection, it will indeed be a point of inflection.</li> <li>- <b>Second Derivative Test:</b> For a <u>critical number</u> <math>c</math>, if <math>f''(c) &lt; 0</math>, then there is a local max at <math>x = c</math>. If <math>f''(c) &gt; 0</math>, then there is a local min at <math>x = c</math>.</li> </ul>